

# CONSISTENCY OF FOREST PRESENCE AND BIOMASS PREDICTIONS MODELED ACROSS OVERLAPPING SPATIAL AND TEMPORAL EXTENTS

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**ABSTRACT.** We assessed the consistency across space and time of spatially explicit models of forest presence and biomass in southern Missouri, USA, for adjacent, partially overlapping satellite image Path/Rows, and for coincident satellite images from the same Path/Row acquired in different years. Such consistency in satellite image-based classification and estimation is critical to national and continental monitoring programs that depend upon processed satellite imagery, such as the North American Forest Dynamics Program. We tested the interchangeability of particular image acquisitions across time and space in the context of modeling forest biomass and forest presence with a non-parametric Random Forests-based approach. Validation at independent USA national forest inventory plots suggested statistically consistent model accuracy, even when the images used to apply the models were acquired in different years or in different image frames from the images used to build the models. For mapping projects using near-anniversary date imagery and employing careful radiometric correction, advantages of image interchangeability include the ability to build models with more ground data by combining adjacent image frames and the ability to apply models of assessed accuracy to early satellite images for which no corresponding field data may be available.

**Keywords:** Consistency analyses, North American Forest Dynamics, NAFD, Landsat, Random Forests, forest inventory, FIA.

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## 1 INTRODUCTION

**1.1 Modeling framework** When field measurements of forest attributes are combined in a modeling or classification framework with synoptic, remotely sensed data to produce spatial products, a fundamental assumption is made. Specifically, it is assumed that the numeric relationship between the forest attribute and the remotely sensed data, as observed at the locations for which field data are available, remains stable across the spatial field over which the attribute is being mapped, provided the inventory plots represent the forest conditions of interest contained within said image in an unbiased manner. At the simplest level, one assumes that a model based on forest inventory plots and a corresponding satellite image may be applied to all the image pixels not sampled by the plots. In this case, care must be taken only to assure that any anomalies (e.g. clouds,

sensor errors) in the remote image are identified and either corrected or excluded. However, when a modeling framework calls for the combination of images from multiple acquisitions, each with their own radiometric and associated vegetation phenological properties, it becomes necessary to standardize the interpretation of remotely sensed values. In this case, all imagery must either be theoretically corrected to some standard absolute scale such as surface reflectance, or the imagery must be empirically cross-calibrated in some way, often using correction factors developed at invariant features where the images overlap. All discussions here will focus on satellite-derived optical reflectance data from passive sensors.

While multiple mapping projects have modeled forest characteristics across large areas using many satellite image frames (e.g., Blackard *et al.*, 2008, Hme *et*

*al.*, 2001, Hansen *et al.*, 2003, Kennedy & Bertolo, 2002, Pivinen *et al.*, 2003, Rufenacht *et al.*, 2008), there is growing impetus to extend models not only over space but also over time (Woodcock *et al.*, 2001). Time series of satellite imagery have the potential to yield uniquely consistent and exhaustive forest change data, particularly if data are acquired from a long-serving platform such as Landsat that has spatial and spectral properties adequate for detecting forest change (Cohen & Goward, 2004).

The North American Forest Dynamics Project (NAFD; see Goward *et al.*, 2008) has initiated work across the USA to apply models of forest biomass to a 25-year (1985–2009) time series of radiometrically corrected Landsat imagery. These models are being calibrated with recent field inventory measurements from the U.S. Forest Service Forest Inventory and Analysis Program (FIA), which is the national forest inventory of the USA. NAFD models are applied to time series of satellite imagery, including dates that precede field inventory data acquisition. The primary goal of NAFD is to describe the effects of disturbance and re-growth on forest carbon stores. A similar approach was taken by Healey *et al.* (2006) to identify forest canopy disturbance in the Pacific Northwest region of the USA. Healey *et al.* (2006) developed a change detection strategy, called “State Model Differencing,” in which mapped pre- and post-disturbance estimates of basal area and percent canopy cover estimates were used to label disturbance magnitude in concrete biophysical terms. This alignment of spectral change signals with traditional forest metrics may in some cases be more useful for forest managers than simple classifications of greater- and lesser-severity events (e.g., Kirschbaum, 2008, Nelson *et al.*, 2009). Powell *et al.* (2010) examined the accuracy of NAFD’s time series maps of forest biomass by using field measurements from multiple points in time. There are also pixel-level temporal smoothing techniques that may be applied to time series of forest condition maps to further reduce year-to-year variation caused by either random error or remaining calibration errors (Powell *et al.*, 2010).

This study was designed to assess whether models of both aboveground standing biomass and forest/non-forest (f/nf) condition would yield predictions of comparable accuracy if the satellite inputs for those models were acquired either in a different place or in a different year than the satellite data used to construct the models originally. While it would be impossible to assess the effects of every possible image artefact on the transferability of forest models from one image frame to another or from one date to the next, the goal of this study was to evaluate the degree to which model accuracy is affected when carefully chosen and calibrated,

near anniversary date imagery is used interchangeably in a modeling project. Application of models across time and space is interpreted as having no impact on model accuracy if statistical tests of model outputs using independent field observations produce non-significant differences at  $\alpha=0.05$ . The objective of this study is to conduct an explicit assessment of the assumed image cross-calibration when the forest modeling frame requires that spectral relationships and models derived from one image be applied to images either from other times or other locations.

Results from this evaluation should be of use to NAFD and other projects that are combining archives of Landsat or similar imagery with forest inventory data across large areas and long time periods.

**1.2 Random Forests** Ensemble approaches to classification and estimation are becoming increasingly popular because ensemble models are often more accurate than individual models (Opitz & Maclin, 1999). Improved classification accuracy is sought by aggregating the classifications of a diverse set of classifiers (Steele, 2000, Zhu, 2010). Ensemble aggregations are obtained by “stacking” multiple predictions, often involving re-sampling of the training dataset (Behrens *et al.*, 2009). Breiman (1996b) described “stacked regressions”, following the idea of stacking in Wolpert (1992). LeBlanc and Tibshirani (1996) suggest that the approach of stacked regressions is identical to the “model-mix” approach proposed earlier by Stone (1974). Chan and Paelinckx (2008) describe ensemble classifications as falling into one of two general categories: 1) those based on a single learning algorithm, but with multiple variations of the training set, and 2) those based on a combination of several different learning algorithms, but with the same training set.

Random Forests (RF; Breiman, 2001), also known as “Breiman Cutler classifications” (BCC; Lawrence *et al.*, 2006) falls within the first ensemble category. RF is a non-linear and non-parametric approach that can address complex multivariate interactions of predictors (Strobl *et al.*, 2008, Strobl *et al.*, 2007). In multi-dimensional data, RF characterizes and exploits structure for the purposes of classification and prediction (Cutler *et al.*, 2007). By permutation of independent variables, RF provides local and global measures of variable importance (Evans & Cushman, 2009).

**1.2.1 RF Classification** Pal (2005) used RF with Landsat 7 Enhanced Thematic Mapper Plus (ETM+) imagery to classify seven agricultural land cover classes in Cambridgeshire, UK. The RF classifier achieved a classification accuracy of 88 percent and a kappa coefficient of 0.86. These results were comparable to those

achieved using the same imagery with a support vector machine classifier (SVM; Vapnik, 2000), but the RF classifier had several operational benefits over the SVM classifier. Using RF with Landsat satellite imagery and ancillary datasets, Prasad et al. (2006) reported kappa coefficients of 0.60 to 0.68 for classifications of four individual tree species in the eastern USA, and Gislason et al. (2006) reported classification accuracies ranging from 28 to 99 percent for nine forest types within Colorado, USA. Gislason et al. (2006) compared the accuracy of RF with other ensemble classifiers, all using Landsat Multispectral Scanner (MSS) satellite remote sensing imagery and geographic data from a mountainous area of Colorado, USA. In terms of accuracies, RF outperformed a single Classification and Regression Tree (CART) classifier and was comparable to accuracies obtained by other ensemble methods (bagging and boosting). Furthermore, RF was much faster than the other ensemble methods, did not overfit, and could be used to estimate the importance of variables and detect outliers.

Cutler et al. (2007) described applications of RF classifier for three ecological presence-absence classifications, including invasive plant species presence in Lava Beds National Monument, California, USA, rare lichen species presence in the Pacific Northwest, USA, and nest sites for cavity nesting birds in the Uinta Mountains, Utah, USA. Five measures of classification accuracies resulting from the RF classifier were compared with those of four other classifiers: linear discriminant analysis, logistic regression, additive logistic regression, and classification trees. For all three presence-absence applications, RF classifications were reported as being moderately to highly superior to the alternate methods tested. Cutler et al. (2007) summarized beneficial characteristics of RF as including, “(1) very high classification accuracy; (??) a novel method of determining variable importance; (??) ability to model complex interactions among predictor variables; (??) flexibility to perform several types of statistical data analysis, including regression, classification, survival analysis, and unsupervised learning; and (??) an algorithm for imputing missing values.”

**1.2.2 RF Estimation** Hudak et al. (2008) compared estimates of two attributes of forest structure - tree density and basal area - for eleven conifer tree species in north-central Idaho, USA, obtained from airborne LiDAR data and imputation techniques based on normalized and unnormalized Euclidean distance, Mahalanobis distance, Independent Component, Canonical Correlation Analysis, Canonical Correspondence Analysis, and RF. Based on scaled root mean square differences, they concluded that RF produced the best overall results.

Baccini et al. (2004) used RF for mapping above-ground forest biomass for National Forest lands of Cali-

fornia, USA. Model R<sup>2</sup> values ranged from 0.68 to 0.75, and 78 percent of predicted values of above-ground forest biomass fell within  $\pm 50$  tons/ha (Baccini et al., 2004). A similar modeling exercise was described in Baccini et al. (2008) for mapping woody above-ground biomass in tropical Africa (Baccini et al., 2008). Using a 10 percent holdout sample of test data, RF models explained 82 percent of variance in above-ground biomass; in comparison, a more traditional, multiple regression analysis explained 71 percent of the variance. In both studies, RF tended to under-predict larger biomass values and over-predict smaller biomass values, likely because regression tree-based model predictions are based on average values within terminal nodes – leaves within a tree-based model that occur when a splitting procedure stops (Baccini et al., 2008).

Powell et al (2010) compared Reduced Major Axis (RMA) regression (Larsson, 1993), Gradient Nearest Neighbor (GNN) imputation (Ohmann & Gregory 2002), and RF regression trees, using Landsat time series stacks for modeling live, aboveground tree biomass in Arizona and Minnesota, USA. For both study areas, the smallest root mean square error (RMSE) values were associated with RF models.

In brief, RF has become a frequently used approach for classification and estimation, including multiple applications involving satellite remote sensing of forest composition and structure. RF is used in this study for modeling aboveground standing biomass and f/nf condition. These models are compared across space and time.

## 2 DATA

**2.1 Study Area** We evaluated models of standing biomass and f/nf condition in three areas of interest within south-central Missouri, USA: 1) The western, non-overlapping portion of Landsat World Reference System 2 (WRS-2) Path 25, Row 34 (P25R34), labelled “W”; 2) The eastern, non-overlapping portion of Path 24, Row 34 (P24R34), labelled “E”; and 3) The area of overlap between P25R34 and P24R34, labelled “O” (Fig. 1). The geographic extent of overlap in O contains image pixels from both P25R34 and P24R34, labelled “WO” and “EO”, respectively. For FIA plots  $WO = O = EO$ .

The study area is located in the Ozark Physiographic Region, in the southern half of Missouri, USA, which is just south of the limit of past glaciations. The ecological units within the study area include the Central Ozark Plateau (222Ab), Current River Hills (222Af), White River Hills (222Ag), and the Springfield Plain (222Am) subsections (Cleland et al., 2007). The Ozark Plateau, Current Hills, and White River Hills subsections are comprised mostly of relatively smooth uplands, with the latter two dissected by downcutting streams

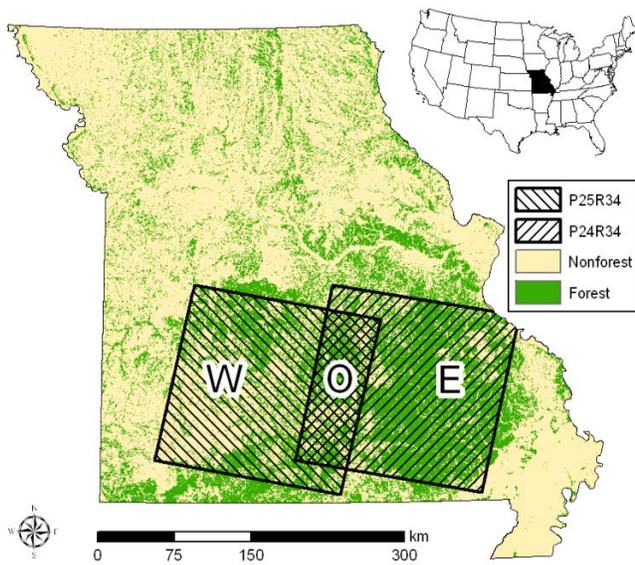


Figure 1: Study areas: Southern Missouri, USA. Data sources: f/nf – USDA Forest Service; base maps – ESRI Data & Maps.

leading to the major rivers. The Springfield plateau is mainly smooth, elevated plains with some dissection due to watercourses (Batek *et al.*, 1999, Foti & Bukenhofer, 1999).

**2.2 FIA Data** FIA defines forest land as lands currently or formerly supporting a minimum level of tree stocking (10 percent) and not developed for a non-forest use such as agriculture, residential, or industrial use. Forest land includes commercial timberland, some pastured land with trees, forest plantations, unproductive forested land, and reserved, noncommercial forested land. FIA’s definition of forest land also requires a minimum area of 0.405 ha and minimum continuous canopy width of 36.58 m (U.S. Department of Agriculture Forest Service, 2003). FIA sample plots follow a nationally consistent configuration comprised of a cluster of four fixed-radius circular subplots, selected from a nationally consistent hexagonal sampling frame with at least one plot selected for each 2400-ha hexagon (Bechtold & Scott, 2005, Reams *et al.*, 2005). On each FIA plot, land use (e.g., proportion forest cover), tree (e.g., species, height, and diameter at breast height: DBH, 1.37 m) and other site variables are collected.

The FIA database was queried to obtain inventory field plot data collected between 1999 and 2007 within all Missouri counties intersecting P25R34 and P24R34. Geographic information system (GIS) data layers of inven-

tory plot center locations were created based on global positioning system (GPS) coordinates obtained during field data collection. GPS coordinates were collected and maintained in North American Datum of 1983. The FIA plots were further constrained to retain only those plots located within the geographic extent of P25R34 or P24R34. FIA plots measured during Missouri cycle 5 (1999-2003) were used for analyses across space ( $n = 2320$ ), with 751 plots within W, 1278 plots within E and 291 plots within O (Fig. 1). P25R34 plots measured during cycle 5 and remeasured during cycle 6 (2004-2007) were used for analyses across time ( $n=735$ ). FIA plots from cycle 6 were not used for modeling within P24R34. For each plot, estimates were produced for 1) proportion forest land; and 2) total aboveground gross biomass oven dry weight per hectare on forest land, based on trees 2.54 cm diameter or larger, including all tops and limbs, but excluding foliage (DRYBIOT in FIA database, hereafter: ‘biomass’). Biomass is calculated as per Heath *et al.* (2008). The mean, range, and standard deviation of per-plot estimates of biomass (Mg/ha) on forest land for each study area were W - 11.65, 33.44, and 6.70; O - 12.19, 32.21, and 6.30; and E - 13.41, 39.15, and 6.45; respectively.

**2.3 Satellite Imagery** WRS-2 Landsat image frames overlap across both “paths,” which reflect the roughly north-south track of the satellites, and “rows”, which are segments of paths approximately 185-km in length. Cross-path comparisons were selected because substantial overlap only exists for adjacent paths (Guindon *et al.*, 2004).

For comparisons across space, a Landsat 5 Thematic Mapper (TM) image was obtained for P25R34, dated 29 August 2000; and a Landsat 7 ETM+ image was obtained for P24R34, dated 30 August 2000 (Fig. 2). Comparisons across time were conducted within P25R34, using the 29 August 2000 TM image and a TM image from 2 September 2007. Resulting images had 28.5-m x 28.5-m spatial resolution and Universal Transverse Mercator (UTM) projection, with North American Datum of 1983. Clouds and cloud shadows, which covered a minimal fraction of the study area, were manually delimited and these areas were excluded from further analyses.

TM and ETM+ data supporting this assessment were converted to surface reflectance by NASA’s Landsat Ecosystem Disturbance Adaptive Processing System (LEDAPS) (Masek *et al.*, 2006). Following conversion of Landsat visible and infrared bands (bands 1-5 and 7) to top-of-atmosphere reflectance, this process uses the MODIS/6S methodology to correct for atmospheric effects. Initial comparisons with ground-based optical thickness measurements and simultaneously acquired MODIS imagery indicate uncertainty in Landsat

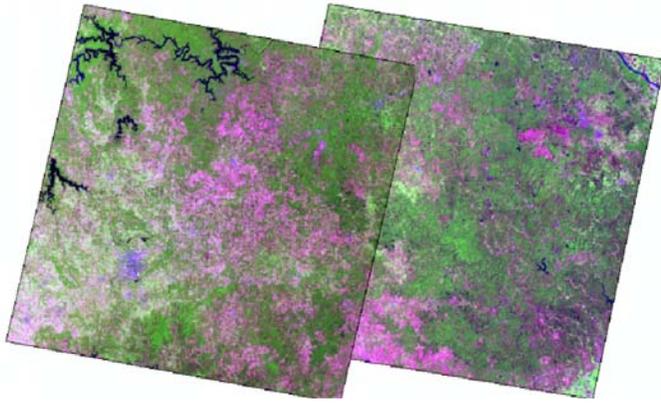


Figure 2: Landsat images of P25R34 (left) and P24R34 (right), late August 2000, southern Missouri, USA.

surface reflectance comparable to the standard MODIS reflectance product (the greater of 0.5 percent absolute reflectance or 5 percent of the recorded reflectance value; Masek, et al., 2006). This pre-processing has been a standard component of the NAFD project (Goward *et al.*, 2008). No further empirical or theoretical normalization was performed.

In addition to Landsat surface reflectance data, two topographic layers were also used for prediction and mapping. The first was elevation from the 1 Arc Second National Elevation Dataset, assembled by the U.S. Geological Survey (<http://seamless.usgs.gov/products/1arc.php>). The second was direct, clear-sky shortwave radiation, which was based on the above elevation dataset and a routine described by Kumar et al. (1997), incorporating a solar date within the range of Landsat acquisitions.

### 3 METHODS

We created models using NAFD image data and assessed their performance using validation input from: 1) the same image as the original model; 2) an adjacent, overlapping Path/Row image from the same year, e.g., performance across space; and 3) the same Path/Row, but from a different year, having a similar anniversary date, e.g., performance across time. Descriptions of the RF modeling process used, as well as the specific tests, are below.

**3.1 Random Forests** RF uses a collection of tree-structured classifiers  $\{h(x, \Theta_k), k = 1, \dots, \}$  where  $x$  is an input pattern and  $\{\Theta_k\}$  are independent identically distributed random vectors. A split for each node is determined by training each tree in RF on a bootstrapped sample of the original training data, across a randomly selected subset of the input variables. For classification,

each tree in the RF casts a unit vote. The most popular class at input  $x$  determines the classification (Breiman, 2001).

RF combines bagging (bootstrap aggregating) with random feature selection for decision trees (Breiman, 2001). Bagging involves the generation of different training sets drawn randomly from the original data set, with replacement, and combining the resulting classifier decisions using a majority vote with equal weight (Breiman, 1996a). Within RF the original sample is partitioned into subsamples, forming node splits until end nodes result, each of which represents a particular class (Watts *et al.*, 2009). Splitting results in a ‘forest’ of classification trees, each of which can differ greatly from the next. Final classification is determined by an ‘among-tree plurality decision’, based on votes cast by each tree in the forest. Out-of-bag (OOB) accuracy measures are produced by withholding a random subset of the original data from the modeling process, and using that OOB data for estimating model accuracy of the classification trees (Lawrence *et al.*, 2006).

Applications of RF for estimation are similar to those described above for classification, but for regression applications, the final prediction is derived from the average of the suite of individual tree outputs (Breiman, 2001).

**3.2 Per-pixel predictions** NAFD protocols include methods for making spatially explicit (map-based) estimates of changes in aboveground forest biomass (Healey *et al.*, 2007, Powell *et al.*, 2010). Per-pixel predictions of biomass and forest probability were produced using RF models. The work reported here was done with R statistical software (R Development Core Team, 2008) using an implementation of RF developed by Liaw and Wiener (2002) and adapted by Freeman and Frescino (2008). This adaptation applies RF models to pixels in a raster image (ERDAS Imagine format) that corresponds to the input satellite imagery. For this approach, 2000 trees were created, with each tree using a different random subset of the data. The number of predictors tried at each node was optimized using the “`tuneRF()`” function (Freeman and Frescino, 2008). These trees were assembled into a ‘forest’ and each tree provided a ‘vote’ on the final, composite tree. Pixels with predictions of forest probability of 0.5 or greater were labelled forest class; all other pixels were labelled non-forest.

**3.2.1 Predictions Across Space** To ensure an adequate number of validation plots in O, which is smaller in geographic area than W or E, we chose a lesser density of training plots and thus a greater density of validation plots. This ratio was reversed for W and E, where geographic extent and numbers of FIA plots were

larger. Sixty percent of the FIA plots within W and E and 40 percent of the FIA plots within O were selected at random as training data for P25R34 models. The remaining 40 percent of plots within W and E ( $n=300$  and  $511$ , respectively) and 60 percent of plots within O ( $n = 175$ ) were retained for validation analyses. A model for P25R34 was applied to: 1) spectral data from WO (i.e., image pixels from the same image for which the model was developed); and 2) spectral data from EO (i.e., image pixels from the adjacent image - P24R34). The same set of FIA validation plots from O was used to assess both applications of the model.

The procedure was duplicated exactly with data from scene E to create predicted maps of biomass and forest proportion in area O using imagery from both W and E, thus allowing for comparison of predictions over the same area made with two different imagery sources. Within O, the same model and validation plots were used for both P25R34 and P24R34 models and validation tests.

**3.2.2 Predictions Across Time** For the year 2000 model, 60 percent of the FIA plots from Missouri cycle 5 (1999-2003) were selected at random for model development and the remaining 40 percent of plots ( $n = 300$ ) were retained for model validation. Similarly, for the year 2007 model, 60 percent of the FIA plots from Missouri cycle 6 (2004-2007) were selected at random for model development and the remaining 40 percent of plots ( $n = 300$ ) were retained for model validation.

A model based on 2000 imagery was applied to: 1) spectral data from 2000 (i.e., image pixels from the same image for which the model was developed); and 2) spectral data from 2007. Similarly, a model based on 2007 imagery was applied to: 1) spectral data from 2007 (i.e., image pixels from the same image for which the model was developed); and 2) spectral data from 2000.

**3.3 Validation** Quantitative assessment of product accuracies is a prerequisite to acceptance and application of image-based classification and estimation products (Congalton, 2004). Areas of overlap between adjacent path/row pairs of satellite images provide not only for “chain classification” of adjacent images (Knorn *et al.*, 2009), but also for quasi-independent validation of classification or estimation. Classification consistency, determined by comparing overlapping portions of individual path/row scenes, can be used as an indicator of classification quality (Cihlar *et al.*, 2003, Guindon & Edmonds, 2004). Extensive image overlap exists for most land resources satellites (e.g., Landsat). In addition to assessing classification consistency, image overlap regions have been used to characterize the accuracy of landscape metrics (Brown *et al.*, 2000) and systematic

surface reflectance and leaf area index (Butson & Fernandes, 2004).

We compared model-based site-specific (per-pixel) classifications of f/nf classification and predictions of biomass with independent ground reference data. When comparing models across space and across time, a naming convention is employed whereby the first term refers to the image source for model development, and the second term refers to the imagery for which models are implemented. Across-space comparisons are termed W-E or E-W, and across-time comparisons are termed 2000-2007, or 2007-2000. Model validation is termed W-W, E-E, 2000-2000, or 2007-2007 when using the same image source for model development and testing.

Site-specific validation tests of f/nf classification were conducted to assess overall classification accuracy and Cohen’s kappa coefficient, both of which are based on a confusion matrix of observed and predicted values (Cohen, 1960). Model predictions were compared to FIA validation plot observations. Kappa analysis provides two statistical tests of significance. The first tests whether a classification (e.g., satellite image-based f/nf classification) is significantly better than a classification generated by randomly assigning class labels to image pixels. In the second Kappa test, confusion matrices from two classification maps can be compared to determine whether they are statistically significantly different from one another (Bishop *et al.*, 1975). Although remotely sensed data are discrete, Cohen’s kappa coefficient is asymptotically normally distributed (Congalton & Green, 2008).

The following test statistics were obtained for the f/nf classification: 1) overall accuracy, 2) maximum likelihood estimate of Kappa, 3) approximate large sample variance of Kappa, 4) significance test of a single confusion matrix, and 5) a test statistic for testing whether two independent confusion matrices are significantly different (Congalton & Green, 2008, Hudson & Ramm, 1987). As for predictions of f/nf class, predictions of biomass were compared to FIA validation plot observations, resulting in estimates of coefficient of determination ( $R^2$ ) and RMSE,

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (\hat{y}_i - y_i)^2} \quad (1)$$

Where  $\hat{y}_i$  is the pixel prediction of biomass for the  $i$ th observation, and  $y_i$  is the plot observation of biomass for the  $i$ th observation in the reference dataset, for  $n$  total observations. RMSE is reported as proportion of mean biomass, noted as RMSEp.

## 4 RESULTS

**4.1 Across Space** Comparing image surface reflectance values collected one day apart, but from different satellite sensors, (Landsat 5 TM vs. Landsat 7 ETM+), we noted the following correlation coefficients for TM/ETM+ bands 1-5 and 7, respectively, for a sample of pixels that contained FIA plot locations: 0.95, 0.96, 0.97, 0.94, 0.97, and 0.97. The three visible bands – 2, 3, and 1, respectively and in order, appeared most important for classifying f/nf, as determined by both mean square error (MSE) and node purity (gini coefficient) (Breiman *et al.*, 1984). For biomass estimation, at least two of the near/mid-infrared bands (4, 5, and 7) appeared among the three most important attributes, both for MSE and for node purity. For both f/nf classification and biomass estimation, the ancillary attributes of elevation and radiation appeared to be the least important attributes, for both MSE and node purity.

Models of f/nf classification for O - the overlapping portion of P24R34 and P25R34 - resulted in area estimates ranging from 44.1 to 50.8 percent for non-forest class and 49.2 to 55.9 percent of forest class (Table 1). Overall accuracy of the f/nf models ranged from 92 to 94 percent, and estimates of Cohen's kappa coefficients ranged from 0.84 to 0.88, with variances ranging from 0.00131 to 0.00164 and Z statistics ranging from 24.2 to 20.8, all of which are statistically significant at the  $\alpha=0.05$  level ( $Z < 1.96$ ) (Table 1).

Pairwise comparisons of f/nf classifications resulted in Z statistics ranging from 0.03 to 0.629, all of which represent statistically non-significant differences at the  $\alpha=0.05$  level ( $Z < 1.96$ ).

Biomass models had R<sup>2</sup> values of 0.72 to 0.74, and RMSEp values of 0.56 to 0.60. In some cases, applying a model based on imagery from one path/row to imagery in the adjacent, overlapping path/row resulted in slightly higher accuracies (Fig. 3).

**4.2 Across Time** Area estimates of non-forest and forest in P25R34 ranged from 60.9 to 61.6 and 38.4 to 39.1 percent of the study area, respectively, for 2000 and 2007 (Table 2). Overall accuracies of f/nf classifications ranged from 88 to 90 percent (Table 2). Cohen's kappa coefficients, variances, and Z statistics ranged from 0.762 to 0.790, 0.00126 to 0.00140, and 20.4 to 22.3, respectively, all of which are statistically significant at the  $\alpha=0.05$  level ( $Z < 1.96$ ) (Table 2).

Z statistics ranged from 0.134 to 0.529 for pairwise comparisons of f/nf classifications for P25R34 during 2000 and 2007, all of which represent statistically non-significant differences at the  $\alpha=0.05$  level ( $Z < 1.96$ ).

Biomass models for P25R34 had R<sup>2</sup> values of 0.74 to 0.79, and RMSEp values of 0.64 to 0.72 (Fig. 4). Differ-

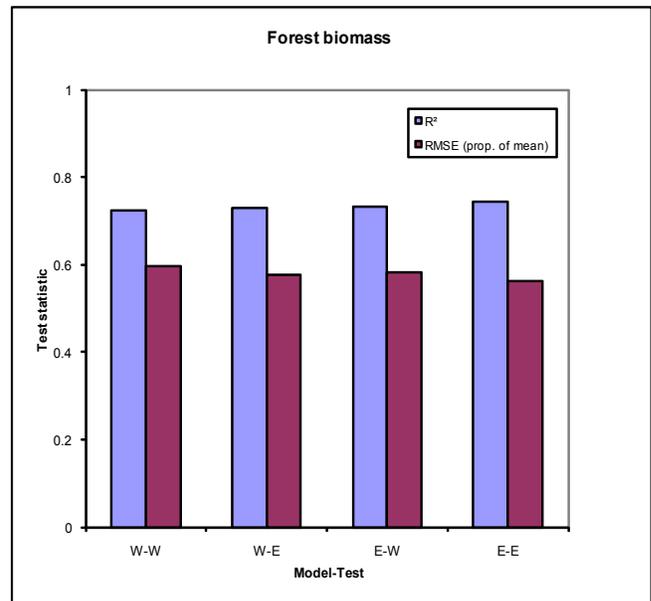


Figure 3: Error metrics for predictions of forest biomass, 2000, southern Missouri, USA.

ences between the models built in 2000 and 2007 were negligible relative to 2000 and 2007 test data. In some cases, the "off year" models were fractionally better than models produced in the same year (Fig. 4).

## 5 DISCUSSION

In this study, satellite-based models of biomass and f/nf classification were applied both to input images used to develop the models and to other images not used to develop the models. Results for overall accuracy of f/nf classification (92 - 94 percent) were among the larger values reported for f/nf classification studies, e.g., 88 percent for a k-Nearest Neighbor classification of f/nf/water in northern Minnesota, USA (Haapanen *et al.*, 2004), and 96 percent for an SVM classification of f/nf in the Carpathian Mountains of central Europe (Knorn *et al.*, 2009). Results for RMSEp (0.56 - 0.60) were similar to, or slightly smaller than reported for other studies, e.g., 0.68 - 0.87 for Arizona, USA and 0.61 - 0.69 for Minnesota, USA study areas (Powell *et al.*, 2010).

No substantial effect on model accuracy was detected for either type of model even though models were tested upon adjacent image frames, different years, and even different sensors (Landsat TM and Landsat ETM+). These results are similar to those reported in Woodcock *et al.* (2001) for Landsat image-based detection of forest change in the Oregon Cascade Range and Colorado Rocky Mountains, USA. It must be noted that all imagery was carefully chosen within a very limited date range to minimize phenological variation, and that state-

Table 1: Comparison of f/nf classifications for models developed using imagery and plot data from either path/row and applied to imagery from the same path/row or to imagery in the same row and adjacent path, 2000, southern Missouri, USA.

Model / Application	Non-forest (%)	Forest (%)	Overall Accuracy (%)	Cohen's Kappa Coefficient	Variance of Kappa	Z Statistic
W-W	44.1	55.9	93.8	0.874	0.00135	23.8
W-E	49.2	50.8	92.1	0.842	0.00164	20.8
E-W	49.7	50.3	93.8	0.876	0.00131	24.2
E-E	50.8	49.2	92.7	0.853	0.00152	21.9

Table 2: Comparison across time of f/nf classifications, Path 25 / Row 34, for models developed using imagery and plot data from either 2000 or 2007 and applied to imagery from the same year and to imagery from the alternate year, southern Missouri, USA.

Model / Application	Non-forest (%)	Forest (%)	Overall Accuracy (%)	Cohen's Kappa Coefficient	Variance of Kappa	Z Statistic
2000-2000	61.3	38.7	89.2	0.783	0.00129	21.8
2000-2007	61.6	38.4	88.9	0.776	0.00133	21.3
2007-2000	60.9	39.1	89.6	0.790	0.00126	22.3
2007-2007	61.6	38.4	88.2	0.762	0.00140	20.4

of-the-art radiometric correction was applied to all imagery. While these conditions undoubtedly contributed to successful transfer of models across image acquisitions, we are encouraged that such measures already are becoming standard procedure in major mapping efforts, e.g., NAFD.

Consistency of these results implies a consistency of both Landsat satellite imagery and FIA data across space and time, even when imagery from two different Landsat sensors was utilized. Results of this study suggest that RF can be used with FIA plot data and Landsat images for modeling f/nf classifications and biomass across time, even for years of imagery when no inventory plot data are available. Furthermore, f/nf classification and biomass prediction appear to be consistent across overlapping image paths, and between Landsat TM and ETM+ images, allowing for flexibility in image selection and compositing over large geographic extents.

The implication of this work is that, at least for forest types similar to those studied here, different image acquisitions may be combined within the same forest modeling framework with little loss of accuracy. Cross-acquisition model stability leads to several operational mapping advantages. Spectral relationships were not tested here across major ecological or edaphic boundaries, but results suggested that at least within ecosystems, scene-by-scene models of forest structure and presence need not be created. Combination of the spectral and field data from adjacent scenes will usually mean

that forest models can be supported by more observations. In many cases, increased training data might be expected to lead to more precise or more robust models. Additionally, for geographic extents containing multiple, semi-overlapping images (e.g., Landsat), precedence can be given to those images with the most desirable characteristics, e.g., least cloud cover or having acquisition date closest to a prescribed anniversary date.

Equally important, results suggested that an assessment of model accuracy using imagery and field data from one time period roughly corresponds to the accuracy of maps created when that same model is applied to properly calibrated imagery from other time periods. This is important because although relatively consistent Landsat imagery is available for many locations since approximately 1985, consistently collected, geo-referenced validation data is rarely available for early dates. In addition to supporting development of maps showing historic forest conditions, application of models to time series of imagery may also enhance forest change detection.

Results here showed that Landsat-based estimates of forest/non-forest were much more accurate than Landsat-based continuous estimates of biomass, an unsurprising outcome since many levels of biomass may exhibit similar canopy reflectance properties whereas the identification of forest is much less dependent upon detection of below-canopy conditions. Based on definitions prescribed for a related study, a threshold was applied

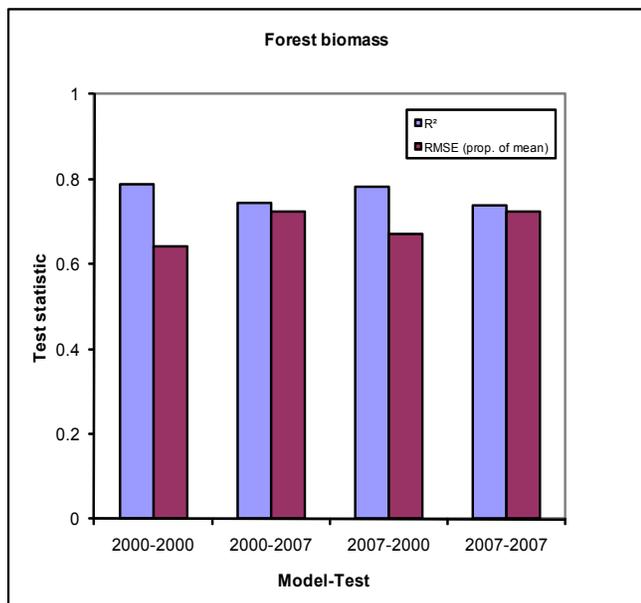


Figure 4: Error metrics for predictions of forest biomass, P25R34, southern Missouri, USA.

to forest probability for labelling as forest those pixels having a probability of 0.5 or greater; all others were labelled non-forest. This “hard” boundary was comparable to using an RF categorical model for classification. In applications outside of the context of the current comparison, however, modeling forest as a continuous probability allows flexible threshold determination in light of classification accuracy based on the kappa statistic, the area under the receiver operating characteristic curve, or a number of other measures.

This study focused on a relatively small geographic extent within central USA. Caution should be exercised when extrapolating these conclusions to other areas. We recommend replication of this study in other geographic regions to test model consistency across space and time.

## 6 CONCLUSIONS

This work confirms that careful image selection and radiometric correction can enable the historical archive of Landsat satellite imagery to be treated interchangeably for the modeling and mapping of forest characteristics. This finding is useful both in the training and validation stages of model- and map-making. If the inclusion of adjacent images in the same modeling frame allows the inclusion of more ground data in the training process, resulting model predictions will presumably tend to be more robust and possibly more precise. There may also be time savings if forest composition and structure do not need to be modeled separately for each individual scene.

The validation advantages of the image interchangeability suggested by this work are particularly acute when models are applied over time. Although comprehensive historical ground data are unavailable in many areas, this work suggests that if images are carefully chosen and calibrated, error rates found in the model-building phase are good indicators of the accuracy of maps that may be created when those models are applied to historic imagery.

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