FORECASTING SUSTAINABILITY:
GROWTH TO REMOVALS RATIO DYNAMICS

Natasha A. James, Robert C. Abt, Karen L. Abt, Raymond M. Sheffield, and Fredrick W. Cubbage

Abstract.—The growth to removals ratio (G/R) is often used as a measure of forest resource sustainability and as a reference point to forecast future resource sustainability. However, little work has been done to determine if any relationship exists between G/R over time. Forest Inventory and Analysis data for 12 southern states were used to determine if any relationship exists between G/R at a given point in time and G/R in the future. Ordinary least squares results indicated a positive relationship over time, meaning a high G/R ratio in the past is associated with a high G/R ratio in the future. However, after removing the effects of differences across space through the use of fixed effects analysis, the results indicated G/R has a negative relationship with itself over time.

INTRODUCTION
The concern of negative anthropogenic impacts on the natural environment and the concerns of insufficient natural resource availability in the future have led to an international agenda to engage in practices leading to resource sustainability and sustainable development. The Montreal Process Criteria and Indicators (MPCI) were developed to address sustainability concerns of the world’s forests. Adopted by 12 countries that represent more than 90 percent of the world’s temperate and boreal forest, these criteria and indicators define seven broad value criteria which are measured by various indicators.

Growth to Removals Ratio
Criterion 2 focuses on maintaining the productive capacity of forest ecosystems. Criterion and Indicator 2.13 focuses specifically on the growth to removals ratio (G/R) (Montreal Process Working Group 2009). Within the field of forest management, resource sustainability is often measured by G/R which is calculated by dividing the net growth in inventory volume during a certain time period by the removals (harvest) within the same time period. A G/R ratio greater than 1 indicates growth in inventory outpaces removals and the resource management within that period could be continued without depleting inventory, and thus is considered sustainable. Although G/R presents a useful snapshot of the relationship of forest growth and removals, it is often used as a means of determining forest sustainability. For example, a high G/R ratio today often is seen as an indicator of a high G/R ratio in the future, thus an assurance of sustainability.

Objective
This study examines G/R for growing stock timberland of both hardwood and softwood species in the selected areas. G/R is calculated as the ratio between net annual growth (the difference between gross growth and mortality) and annual removals for timberland. Figures 1-3 depict G/R over time for each state used in this analysis. Although Kentucky is part of the southern FIA, it was not included due to insufficient data.
Even though it is common practice to use a G/R ratio greater than 1 as an indicator of continued sustainability in the future, Figures 1-3 show a relationship over time where periods of low G/R are followed by periods of high G/R, suggesting a cyclical, negative relationship (Sheffield 2012). The objective of this study was to investigate how well G/R in the past explains G/R today.

Figure 1.—G/R ratio over time for southern states bordering the Gulf of Mexico.

Figure 2.—G/R ratio over time for southern states bordering the Atlantic coast.
DATA

The data used in this analysis were extracted from the Forest Inventory and Analysis (FIA) database. Data relating to annual removals and net growth were collected at the survey unit level for the 12 southern states. Although net growth and annual removals are estimates containing their own standard errors, for the purposes of this paper they are both being treated as population values.

Historically, the FIA Program collected data using a 10-year periodic survey. In 1998, the Agricultural Research, Extension, and Education Reform Act (PL 105-185) required an annual inventory. However, the panel design described by Bechtold and Patterson (2005) was implemented. This panel design allows federal funding for a 10 panel design in the East. Many southern states use a 5 panel design in which 20 percent of plots within a state are sampled each year, creating full inventory reports in 5-year cycles (Smith and Oswalt 2010).

Due to the inconsistency in survey dates, the years in which surveys took place were divided into the following periods:

- Period 1: 1970-1978
- Period 2: 1979-1987
- Period 3: 1988-1993
- Period 4: 1994-2003
- Period 5: 2004-2008
- Period 6: 2009-2010

METHODS

Ordinary least squares (OLS) analysis was used to determine if any relationship exists between G/R today and in the past. In this analysis, each period for each state is a single observation. In addition, fixed effects analysis was applied which controls for the average differences across space (states) in order to observe only the effects of time on G/R. In this analysis, the cross section was defined as the state and the time

3 Florida had 2 surveys during Period 2 (1980 and 1987). The 1987 survey data are included in Period 3.
series was defined in periods, as shown above. The models analyzed for both procedures were:

Model 1: \( (G/R)_T = f ((G/R)_{T-1}) \)

Model 2: \( (G/R)_T = f ((G/R)_{T-2}) \)

Model 3: \( (G/R)_T = f ((G/R)_{T-1}, (G/R)_{T-2}) \)

where \((G/R)_T\) is G/R of the current period; \((G/R)_{T-1}\) is G/R lagged one period; and \((G/R)_{T-2}\) is G/R lagged two periods.

RESULTS AND DISCUSSION

Three OLS models and three fixed effects models were used to examine the relationship G/R has with itself over time. The first model focuses on the relationship between G/R of the current period and the G/R lagged one period. The second model focuses on the relationship between G/R of the current period and the G/R lagged two periods. The final model focuses on the relationship between G/R of the current period and the G/R lagged one and two periods. Results from OLS and fixed effects analysis are listed in Table 1 and Table 2, respectively.

In each model the parameter coefficients are positive and significant at the 1 percent level. This result suggests G/R has a positive relationship with itself over time. However, the R² values are relatively low, ranging from 0.14-0.24.

Through the use of fixed effects analysis, the average differences across states are isolated to determine whether G/R at a point in time has implications for determining G/R in the future. In each model, the F statistic \((F_{stat})\) is significant at the 5 percent level, indicating there are group effects across space and that OLS would not be expected to produce reasonable results. Although the R² values are higher (0.55-0.72), the relationship between G/R today and its values lagged one period and two periods (Model 1 and 2) lack significance even at the 20 percent level. However, when analyzed simultaneously (Model 3), \((G/R)_{T-1}\) and \((G/R)_{T-2}\) show a significant, negative relationship with G/R of the current period. This result implies an inverse relationship where the higher G/R is in the past, the lower it will be in the future.

CONCLUSION AND FUTURE WORK

The results from this study show that when controlling for the average differences across space, empirical evidence suggests that G/R has a negative relationship with itself over time. This analysis is just one of many steps in understanding G/R. In the South, the G/R is rarely below 1. Future work should include regions where G/R is not as stable. Future analysis should include examination of hardwoods and softwoods separately, as these ratios can be different over time.

### Table 1.—Results from Ordinary Least Squares (OLS) analysis of G/R on lagged values of G/R for 12 southern states (standard errors in parentheses)

<table>
<thead>
<tr>
<th></th>
<th>Model 1</th>
<th>Model 2</th>
<th>Model 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>0.83</td>
<td>0.96</td>
<td>0.74</td>
</tr>
<tr>
<td>((G/R)_{T-1})</td>
<td>0.45***</td>
<td>0.30***</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.08)</td>
<td>(0.10)</td>
<td></td>
</tr>
<tr>
<td>((G/R)_{T-2})</td>
<td>0.32***</td>
<td>0.16***</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.09)</td>
<td>(0.10)</td>
<td></td>
</tr>
<tr>
<td>Number of observations</td>
<td>102</td>
<td>78</td>
<td>78</td>
</tr>
<tr>
<td>Adjusted R²</td>
<td>0.24</td>
<td>0.14</td>
<td>0.23</td>
</tr>
</tbody>
</table>

Note: ***indicates significance at 1%.

### Table 2.—Results from fixed effects analysis G/R on lagged values of G/R for 12 southern states (standard errors in parentheses)

<table>
<thead>
<tr>
<th></th>
<th>Model 1</th>
<th>Model 2</th>
<th>Model 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>1.91</td>
<td>2.02</td>
<td>2.63</td>
</tr>
<tr>
<td>((G/R)_{T-1})</td>
<td>-0.10*</td>
<td>-0.33***</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.14)</td>
<td>(0.14)</td>
<td></td>
</tr>
<tr>
<td>((G/R)_{T-2})</td>
<td>-0.18</td>
<td>0.21*</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.15)</td>
<td>(0.14)</td>
<td></td>
</tr>
<tr>
<td>Number of cross sections</td>
<td>12</td>
<td>12</td>
<td>12</td>
</tr>
<tr>
<td>Time series length</td>
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<td>4</td>
<td>4</td>
</tr>
<tr>
<td>Adjusted R²</td>
<td>0.55</td>
<td>0.66</td>
<td>0.72</td>
</tr>
</tbody>
</table>

* ***indicates significance at 1%, * indicates significance at 20%.
In addition, stronger statistical analyses such as spectral analysis or Fourier regression could be applied to determine cyclical relationships.

ACKNOWLEDGMENTS

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LITERATURE CITED


